

14. The diagram indicates that  $AD = BD = 3$  and  $AC = 8$ . Since  $CD$  is the perpendicular bisector of  $BA$ , we know that  $AC = BC = 8$  by the Perpendicular bisector theorem.

The perimeter of  $\triangle ABC = 3 + 3 + 8 + 8 = 22$ .

15. The diagram indicates that  $BC = 10$ ,  $AB = 7$  and the perimeter of  $\triangle ABC$  is 27. First, solve for the unknown length  $AC$ .

$$AB + BC + AC = 27$$

$$10 + 7 + AC = 27$$

$$AC = 10$$

Since  $AC = BC$ ,  $CD$  is the perpendicular bisector of  $BA$  and  $BD = AD$  by the Converse of the Perpendicular Bisector Theorem. Thus, solve for  $BD$ .

$$BD + AD = AB$$

$$BD + BD = 7$$

$$BD = 3.5$$

16. Since  $BF = DF$ , by the Converse of the Perpendicular Bisector Theorem  $FC \perp BD$  and  $BC = CD$ . Since  $FC$  is along the same line as  $AC$ , it follows that  $AC \perp BD$ . Thus,  $AD = AB$  by the Perpendicular Bisector Theorem. So  $AD = AB = 21$ .

17. Given  $EB = ED = 6.2$ , apply the Converse of the Perpendicular Bisector Theorem to find that  $DC = CB$ . Given that  $CD = 3.3$ , solve for  $BD$ .

$$BD = DC + CB$$

$$= 3.3 + 3.3$$

$$= 6.6$$

18. Given  $YW = WZ = 5$ , it follows that  $m\angle YXW = m\angle WXZ$  by the Converse of Angle Bisector Theorem. Given  $m\angle YXW = 21^\circ$ , find  $m\angle ZXY$ .

$$m\angle ZXY = m\angle YXW + m\angle WXZ$$

$$= 21^\circ + 21^\circ$$

$$= 42^\circ$$

19. Given  $m\angle YXZ = 38^\circ$  and  $m\angle WXZ = 19^\circ$ , solve for  $m\angle YXW$ .

$$m\angle WXZ + m\angle YXW = m\angle YXZ$$

$$19^\circ + m\angle YXW = 38^\circ$$

$$m\angle YXW = 19^\circ$$

Thus,  $m\angle WXZ = m\angle YXW$ . By the Angle Bisector Theorem,  $WZ = YW$ .

Given  $WZ = 8.1$ ,

$$WZ = YW = 8.1.$$

20. Since  $CD = 4$  and  $AC = AE$ , we know that  $CD = DE$  by the Converse of the Perpendicular Bisector Theorem. Thus,  $CD = DE = 4$ . Given that the perimeter of  $\triangle ABCC$  is 23 and knowing  $AC = AE$ , we solve for the perimeter of  $\triangle ABC$

$$\text{Perimeter: } 23 + CD + CE = 23 + 4 + 4 = 31$$

21. Given:  $\angle ACF \cong \angle ECF$ ,  $\angle ABF$  and  $\angle EDF$  are right angles.

Prove:  $\triangle ABF \cong \triangle EDF$

Statement	Reason
1. $\angle ACF \cong \angle ECF$	1. Given
2. $\angle ABF$ and $\angle EDF$ are right angles.	2. Given
3. $BF = DF$	3. Angle Bisector Theorem
4. $\overline{BF} \cong \overline{DF}$	4. Definition of congruent segments
5. $\angle ABF \cong \angle EDF$	5. Right angles are congruent.
6. $\angle BFA \cong \angle DFE$	6. Vertical angles theorem
7. $\triangle ABF \cong \triangle EDF$	7. Angle-Side-Angle (ASA)

22. The lower-left side and the lower-right side have equal lengths by the perpendicular bisector theorem. The upper-left side and the upper-right side also have equal lengths by the perpendicular bisector theorem. So the perimeter of the garden is  $12 + 12 + 14 + 14 = 52$  feet.
23.  $\angle FCE$  is cut at  $23^\circ$ ; to solve for the angle she should cut, first solve for  $m\angle EFC$ .

Since  $\angle BFE$  and  $\angle EFC$  make up a straight angle, the sum of the two angles equals  $180^\circ$ . Given  $m\angle BFE = 90^\circ$ , we know that  $m\angle EFC = 90^\circ$ .

Solve for  $m\angle CEF$ .

We know that  $m\angle DEB = m\angle BEF$  by the Converse of Angle Bisector Theorem. Therefore,  $m\angle DEB = m\angle BEF = 31^\circ$ .

Since  $\angle EDB$  and  $\angle ADE$  make up a straight angle, the sum of the two angles equals  $180^\circ$ . Given that  $m\angle EDB = 90^\circ$ , we know that  $m\angle ADE = 90^\circ$ .

We can then solve for  $m\angle DEA$  and use the definition of straight angle to solve for  $m\angle CEF$ .

$$m\angle DEA + m\angle ADE + m\angle EDA = 180^\circ$$

$$m\angle DEA + 90^\circ + 39^\circ = 180^\circ$$

$$m\angle DEA = 51^\circ$$

$$m\angle DEA + m\angle DEB + m\angle FEB + m\angle CEF = 180^\circ$$

$$51^\circ + 31^\circ + 31^\circ + m\angle CEF = 180^\circ$$

$$m\angle CEF = 67^\circ$$

Use  $m\angle EFC$  and  $m\angle CEF$  to solve for  $m\angle FCE$ .

$$m\angle EFC + m\angle CEF + m\angle FCE = 180^\circ$$

$$67^\circ + 90^\circ + m\angle FCE = 180^\circ$$

$$m\angle FCE = 23^\circ$$

Therefore, triangle  $\triangle EFC$  should be cut with angle measures of  $23^\circ$ ,  $67^\circ$ , and  $90^\circ$ .

25.

	Yes	No	Explanation
$AP = XP$		x	$AP$ is not given.
$AB = XY$		x	$AB$ and $XY$ are not given.
$AP = BP$		x	$AP$ is not given.
$XB = YB$	x		Perpendicular Bisector Theorem
$AY = XB$		x	The points $A$ and $B$ are not necessarily equidistant from $X$ and $Y$ .
$XP = YP$	x		Point $P$ is the midpoint of $\overline{XY}$ .

26.

The points  $G$ ,  $J$ , and  $K$  form an isosceles triangle. In an isosceles triangle, the sides opposite the legs are congruent. This means that  $\angle GJP \cong \angle GKP$ . We already know that  $GJ = GK$ . In order to use the angle bisector theorem, we need  $\angle JGK \cong \angle KGP$ . In order for this to be true,  $\angle GPJ$  must be a right angle.